

2-7

Skills Practice***Proving Segment Relationships***

Justify each statement with a property of equality, a property of congruence, or a postulate.

1. $QA = QA$ *Reflexive Property*

2. If $\overline{AB} \cong \overline{BC}$ and $\overline{BC} \cong \overline{CE}$, then $\overline{AB} \cong \overline{CE}$.

Transitive Property

3. If Q is between P and R , then $PR = PQ + QR$.

Segment Addition Postulate

4. If $AB + BC = EF + FG$ and $AB + BC = AC$, then $EF + FG = AC$.

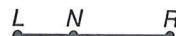
Substitution

Complete each proof.

5. Given: $\overline{SU} \cong \overline{LR}$
 $\overline{TU} \cong \overline{LN}$



Prove: $\overline{ST} \cong \overline{NR}$



Proof:

Statements

a. $\overline{SU} \cong \overline{LR}$, $\overline{TU} \cong \overline{LN}$

b. $SU = LR$, $TU = LN$

c. $SU = ST + TU$

$$LR = LN + NR$$

d. $ST + TU = LN + NR$

e. $ST + LN = LN + NR$

f. $ST + LN - LN = LN + NR - LN$

g. $ST = NR$

h. $\overline{ST} \cong \overline{NR}$

Reasons

a. Given

b. Definition of \cong segments

c. Segment Addition Postulate

d. Substitution

e. Substitution

f. Subtraction Property

g. Substitution Property

h. Definition of Congruent Segments

6. Given: $\overline{AB} \cong \overline{CD}$

Prove: $\overline{CD} \cong \overline{AB}$

Proof:

Statements

a. $\overline{AB} \cong \overline{CD}$

b. $AB = CD$

c. $CD = AB$

d. $\overline{CD} \cong \overline{AB}$

Reasons

a. Given

b. Definition of \cong segments

c. Symmetric Property

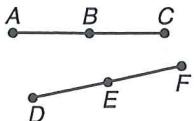
d. Definition of \cong segments

2-7 Practice**Proving Segment Relationships**

Complete the following proof.

1. Given: $\overline{AB} \cong \overline{DE}$
 B is the midpoint of \overline{AC} .
 E is the midpoint of \overline{DF} .
- Prove: $\overline{BC} \cong \overline{EF}$

Proof:



Statements	Reasons
a. $\overline{AB} \cong \overline{DE}$ B is the midpoint of \overline{AC} . E is the midpoint of \overline{DF} .	a. Given
b. $AB = DE$	b. Definition of \cong segments
c. $AB = BC$ $DE = EF$	c. Definition of Midpoint
d. $AC = AB + BC$ $DF = DE + EF$	d. Segment Addition Postulate
e. $AB + BC = DE + EF$	e. Substitution Property
f. $AB + BC = AB + EF$	f. Substitution Property
g. $AB + BC - AB = AB + EF - AB$	g. Subtraction Property
h. $BC = EF$	h. Substitution Property
i. $\overline{BC} \cong \overline{EF}$	i. Definition of \cong segments

2. TRAVEL Refer to the figure. DeAnne knows that the distance from Grayson to Apex is the same as the distance from Redding to Pine Bluff. Prove that the distance from Grayson to Redding is equal to the distance from Apex to Pine Bluff.

Given: $\overline{GA} \cong \overline{RP}$ Prove: $\overline{GR} \cong \overline{AP}$

Statements	Reasons
1. $\overline{GA} \cong \overline{RP}$	1. Given
2. $GA = RP$	2. Definition of \cong segments
3. $GA + AR = AR + RP$	3. Addition Property
4. $GR = GA + AR$, $AP = AR + RP$	4. Segment Addition Postulate
5. $GR = AP$	5. Substitution Property
6. $\overline{GR} \cong \overline{AP}$	6. Definition of \cong segments