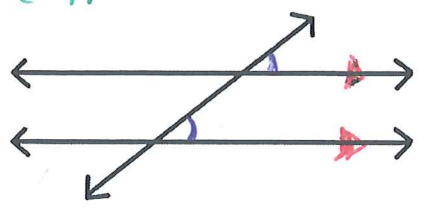
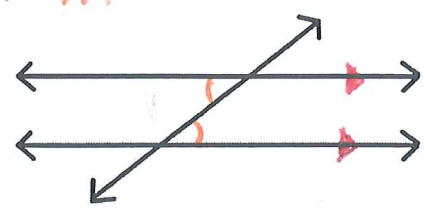
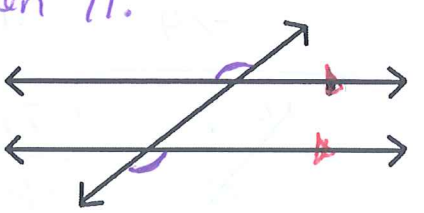
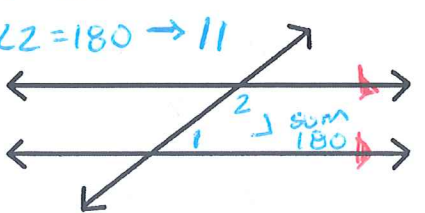
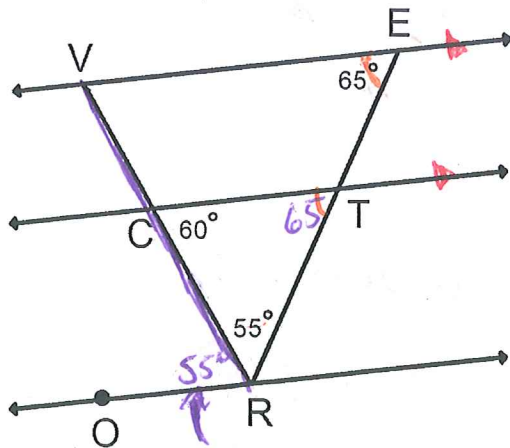


## Geometry - 3.5 - Proving Lines are Parallel

<p style="color: green;">Converse Corresponding <math>\angle</math>'s</p> <p style="color: green;">IF corr. <math>\angle</math>'s are <math>\cong</math> then <math>\parallel</math></p> 	<p style="color: orange;">Converse of (AIA)</p> <p style="color: orange;">IF AIA are <math>\cong</math> then <math>\parallel</math>.</p> 
<p style="color: purple;">Converse AEA</p> <p style="color: purple;">IF AEA are <math>\cong</math> then <math>\parallel</math>.</p> 	<p style="color: blue;">Converse of (CIA)</p> <p style="color: blue;">IF CIA are supplementary then <math>\parallel</math>.</p> <p style="color: blue;"><math>\angle 1 + \angle 2 = 180 \rightarrow \parallel</math></p> 

**Ex 1** - In the figure below,  $\overline{RV}$  bisects  $\angle ORE$ . Determine which lines, if any, are parallel.



Def of  $\angle$  Bisector

$$55 + 55$$

$$110$$

$$\begin{array}{r} 110 \\ + 65 \\ \hline 175 \end{array}$$

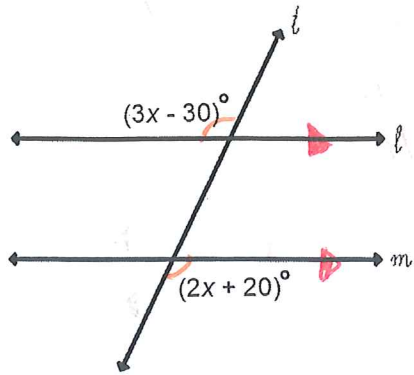
$$\begin{array}{r} 60 \\ 55 \\ \hline 115 \end{array}$$

$$\begin{array}{r} 115 + x = 180 \\ - 115 \quad - 115 \\ \hline \end{array}$$

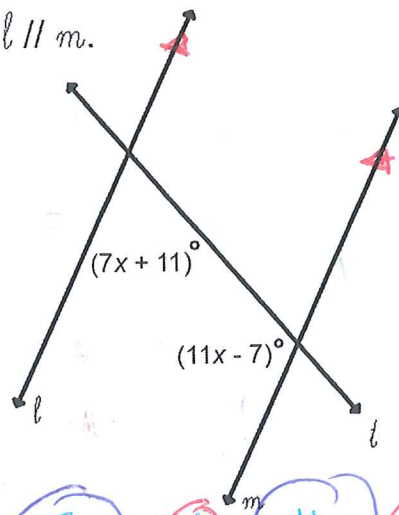
$$x = 65$$

$\overleftrightarrow{VE} \parallel \overleftrightarrow{CT}$  by converse  
of Corr.  $\angle$ 's  
 $\overleftrightarrow{OR} \parallel \overleftrightarrow{CT}$  by Converse  
of CIA.

**Ex 2** - In the figures below, find  $x$  so that  $l \parallel m$ .



$$\begin{aligned} 3x - 30 &= 2x + 20 \\ +30 &\quad +30 \\ \hline 3x &= 2x + 50 \\ -2x &\quad -2x \\ \hline x &= 50 \end{aligned}$$

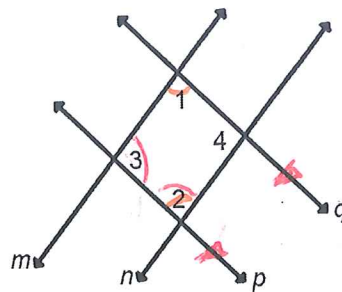


$$\begin{aligned} (7x + 11) + (11x - 7) &= 180 \\ 18x + 4 &= 180 \\ -4 &\quad -4 \\ \hline 18x &= 176 \\ \frac{18x}{18} &= \frac{176}{18} \end{aligned}$$

**Ex 3:**

Given:  $p \parallel q$   
 $\angle 1 \cong \angle 2$

Prove:  $m \parallel n$



$$x = \frac{88}{9}$$

- ①  $p \parallel q$ ,  $\angle 1 \cong \angle 2$
- ②  $m\angle 1 + m\angle 3 = 180$
- ③  $m\angle 1 = m\angle 2$
- ④  $m\angle 2 + m\angle 3 = 180$
- ⑤  $m \parallel n$

- ① Given
- ② Def CIA
- ③ Def of  $\cong$   $\angle$ 's
- ④ Substitution
- ③ Converse of CIA