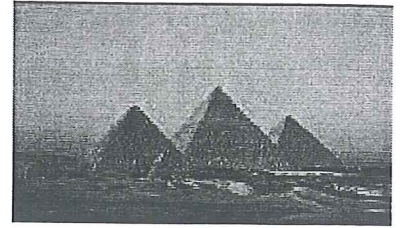
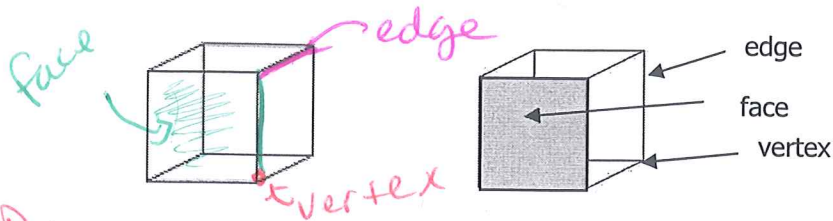


This is a photo of the pyramid of Menkaure in Giza, Egypt. It is an example of a **polyhedron**.



A solid with all flat surfaces that enclose a single region of space is called a polyhedron. Each flat surface, called a faces, is a

polygon. The line segments where the faces intersect are called edges. Edges intersect at a point called a vertex.



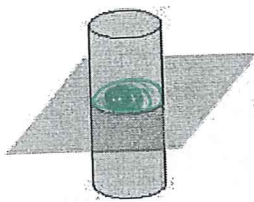
A Prism is a polyhedron with two parallel congruent faces called bases. The other faces are **parallelograms**. Name each prism by its **bases**. A regular prism has bases that are regular polygons.

Name	<u>Triangular</u> Prism	<u>Rectangular</u> Prism	<u>Pentagonal</u> Prism
Model			
Shape of bases	<u>Triangle</u>	<u>Rectangle</u>	<u>Pentagon</u>

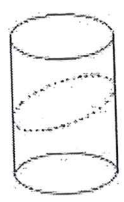
A polyhedron with all faces (except for one) intersecting at one vertex is a pyramid, which are named for their bases, which can be any polygon.

NOT Polyhedrons			
Name	Cylinder	Cone	Sphere
Model			
Description	≅ circular bases in a pair of parallel planes	circular base and vertex	set of points in space that are a given distance from a given point

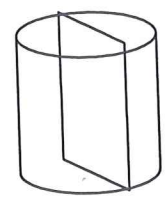
A Cross section is a "slice" of a solid.



Cross section: Circle

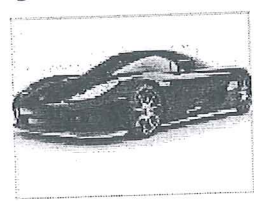


Slice: Oval

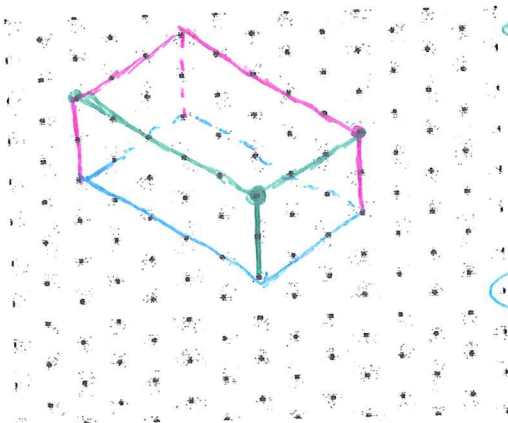


Slice: Rectangle

Surface area is important to car manufacturers because modifying surface area can help the aerodynamics of a car. Modifying surface area can increase speed and efficiency.

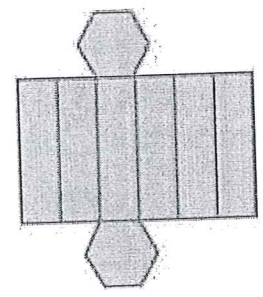
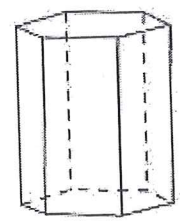
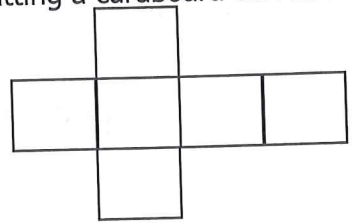
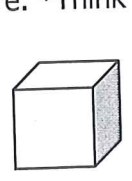


Steps for drawing a rectangular prism 2 units high, 5 units long, and 3 units wide.



- Step 1: Draw the corner. 2 units down, 5 units to left, 3 to right
- Step 2: Draw a parallelogram for the top of the solid
- Step 3: Draw segments 2 units down from each vertex for edges
- Step 4: Connect the corresponding vertices. Use dashed lines for hidden edges. Shade the top of the solid.

A Net is a pattern for a three-dimensional solid. Nets can be made for any solid figure. *Think of cutting a cardboard box at the edges and laying it flat.

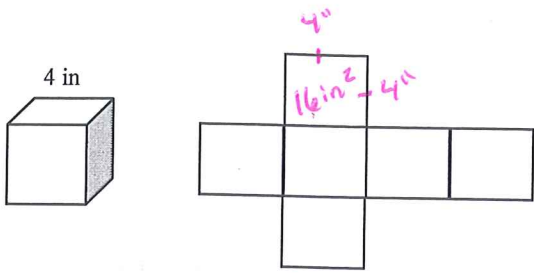


PRISMS

- The bases are congruent faces in parallel planes.
- The faces that are not bases are called lateral faces.
- The lateral faces intersect at the lateral edges.
- Lateral edges are parallel segments.
- A segment perpendicular to the bases with an endpoint in each plane is called an altitude of the prism. Height = Altitude.
- A prism with lateral edges that are also altitudes is called a right prism.
- If lateral edges are not perpendicular to the bases, it is an oblique prism.
- Lateral area, L , is the sum of the areas of the lateral faces.

One way to find the **Surface Area** (T) of a solid is to draw the net, find the area of each 2-dimensional surface, and then add the areas together. Find the surface area of the cube and the right regular hexagonal prism.

$$A = \frac{1}{2} P \cdot a$$



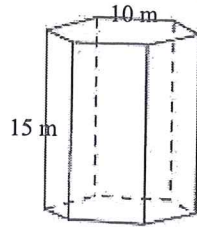
$$16 \text{ in}^2 \times 6$$

$$96 \text{ in}^2$$

$$\frac{1}{2} \cdot 5\sqrt{3} \cdot 60 = 259.8 \text{ m}^2$$

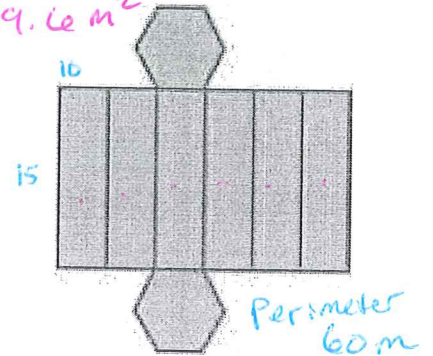
$$\times 2$$

$$519.6 \text{ m}^2$$



$$150$$

$$\times 6$$

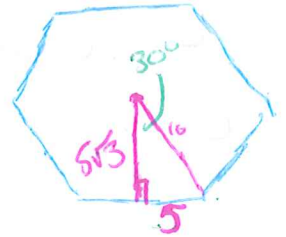


What is the **Lateral Area** (L) of the hexagonal prism?

$$900 \text{ m}^2$$

$$900 \text{ m}^2 + 519.6 \text{ m}^2$$

$$1,419.6 \text{ m}^2$$



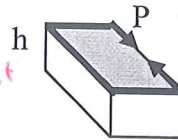
LATERAL AREA OF A PRISM (using a Formula)

Another way to find the Lateral or Surface area of a right prism is to use a formula.

If a right prism has a lateral area of L square units, a height of h units, and each base has a perimeter of P units, then

$$L = P \cdot h$$

↑ Lateral Surface Area
↑ Perimeter
↑ height



$$L = 60 \cdot 15$$

$$L = 900 \text{ m}^2$$

SURFACE AREA OF A PRISM (using a Formula)

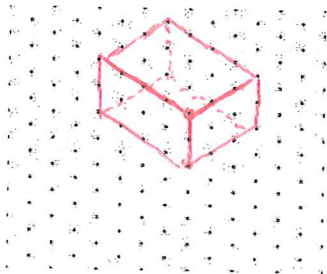
If the surface area of a right prism is T square units, its height h units, and each base has an area of B square units, and a perimeter of P units, then

$$T = L + 2B$$

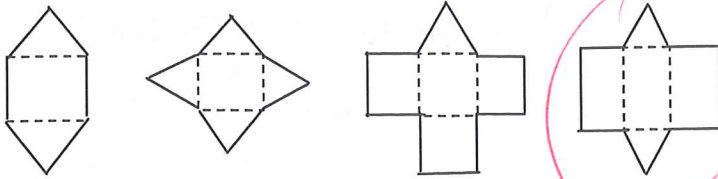
↑ Surface Area
↑ Lateral Surface Area
↑ Area of the Base

Example Problems

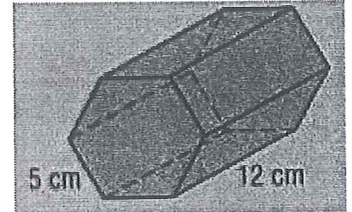
1. Sketch a rectangular prism 4 units long, 3 units wide, and 2 units high using the given isometric dot paper.



2. Which net could be folded into a triangular prism if folds are made only along dotted lines?



3. Find the lateral area of the regular hexagonal prism. (Use a formula.)

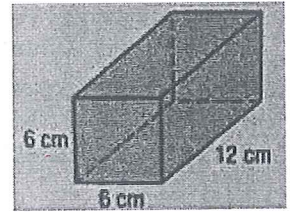


$$L = P \cdot h$$

$$L = 30 \text{ cm} \cdot 12 \text{ cm}$$

$$L = 360 \text{ cm}^2$$

4. Find the surface area of the square prism. (Use a formula.)



$$L = 24 \text{ cm} \cdot 12 \text{ cm}$$

↑
Perimeter
of
Base

↑
height

$$T = L + 2(B)$$

↑
Surface
area

↑
Area
of
Base

$$T = 360 \text{ cm}^2$$

$$L = 288 \text{ cm}^2$$

$$T = 288 \text{ cm}^2 + 2 \cdot 36$$

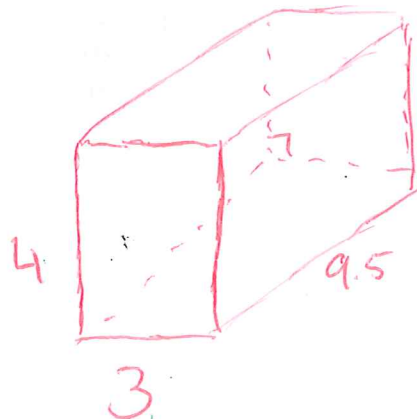
$$T = 288 \text{ cm}^2 + 72 \text{ cm}^2$$

5. A solid block of marble will be used for a sculpture. If the block is 3 feet wide, 4 feet long, and 9.5 feet high, find the surface area of the block. (Use a formula.)

$$P = 14 \text{ ft}$$

$$L = 14 \text{ ft} \cdot 9.5$$

$$L = 133 \text{ ft}^2$$



$$T = L + 2(B)$$

$$T = 133 \text{ ft}^2 + 2(3 \cdot 4)$$

$$= 133 \text{ ft}^2 + 2(12)$$

$$133 \text{ ft}^2 + 24$$

$$= 157 \text{ ft}^2$$